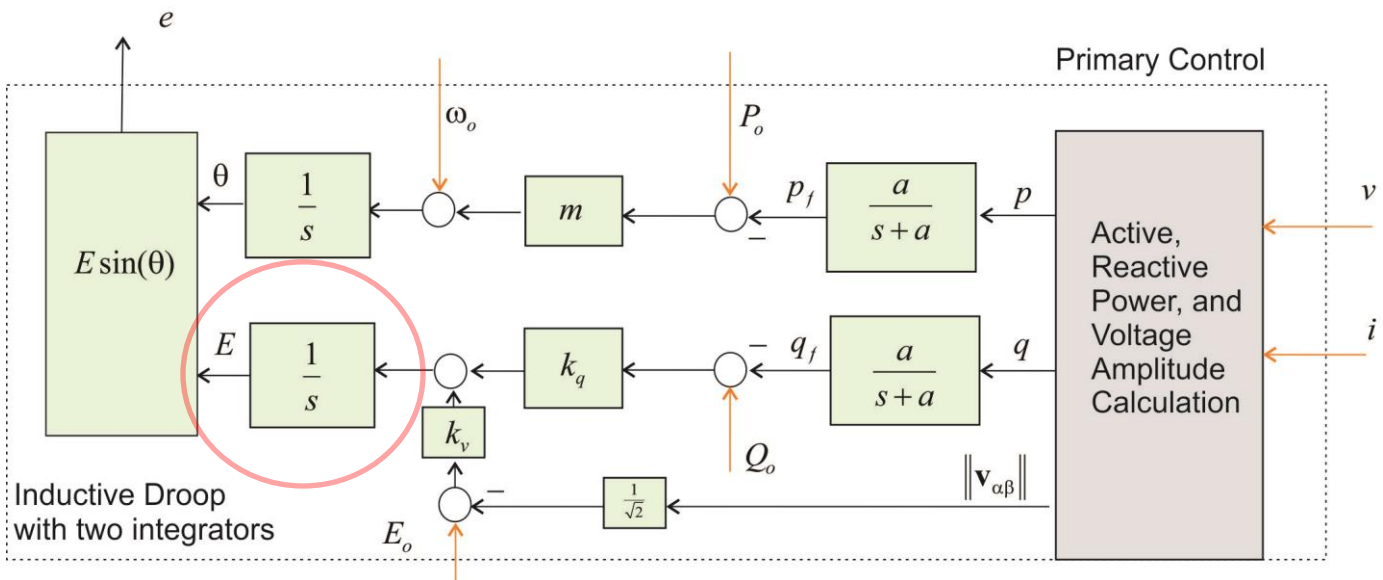
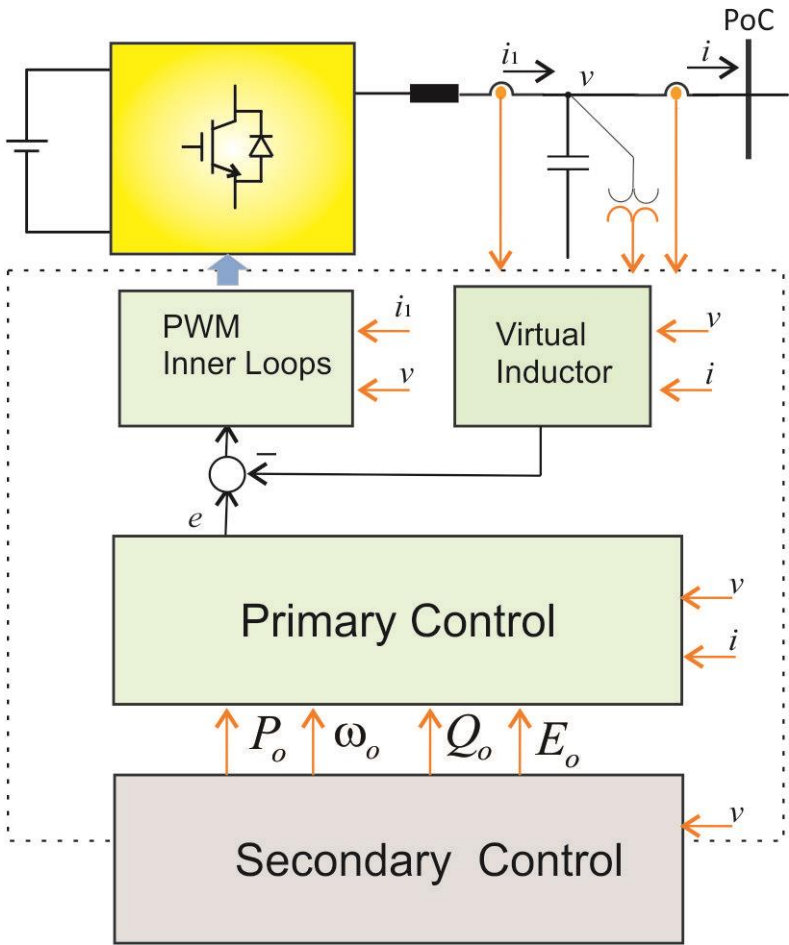


# Grid-Forming Inverter with Inductive Droop Control

Integrator in the reactive power – voltage loop



# Dynamic model – Grid-Forming Inverter with inductive droop

Integrator is added in the reactive power – voltage loop

$$\frac{d\delta}{dt} = \omega + b_{11}$$

$$\frac{d\omega}{dt} = a_{21}\omega + a_{22}e \sin(\delta) + b_{21}$$

$$\frac{de_d}{dt} = a_{21}e_d + a_{32}e \cos(\delta) + b_{31}$$

$$\frac{de}{dt} = e_d$$

$$b_{11} = -\omega_r$$

$$a_{21} = -a$$

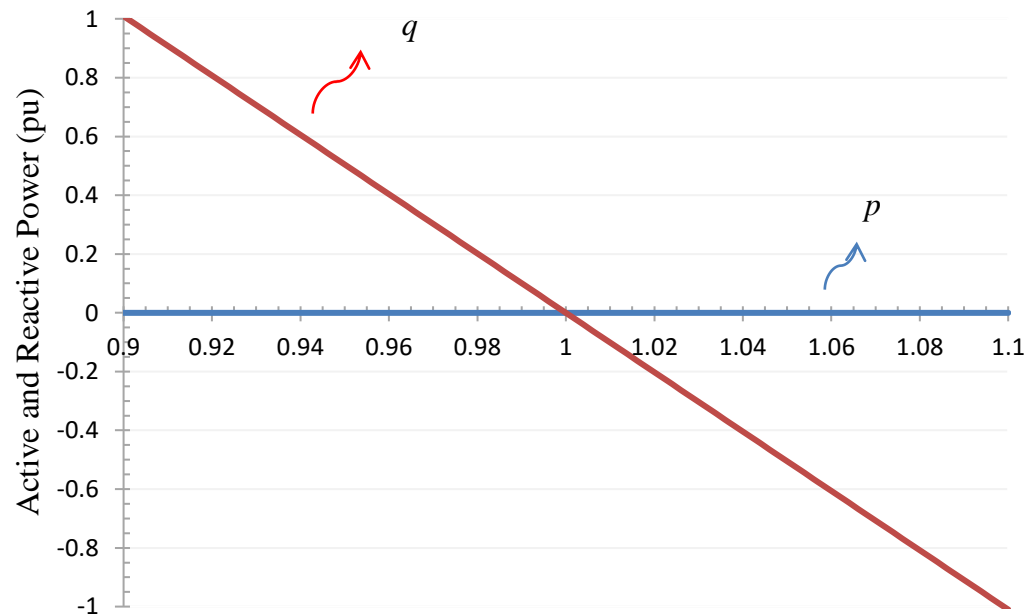
$$b_{21} = a[\omega_o + mP_o]$$

$$a_{32} = -\frac{k_q a V}{X_L}$$

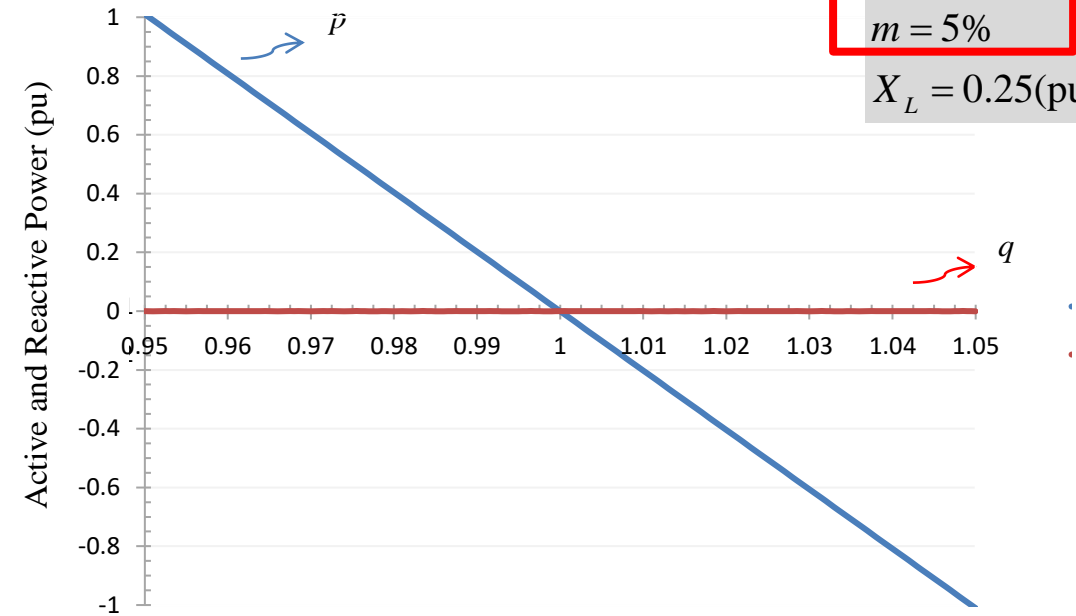
$$b_{31} = k_q a \left[ Q_o + \frac{V^2}{X_L} + \frac{1}{n} (E_o - V) \right]$$

$$n = \frac{k_q}{k_v}$$

# Steady-State Performance



Voltage at the PoC (pu)



Frequency at the PoC (pu)

$E_o = 1$   
 $\omega_o = 1$   
 $P_o = 0$   
 $Q_o = 0$   
 $n = 10\%$   
 $m = 5\%$   
 $X_L = 0.25(\text{pu})$

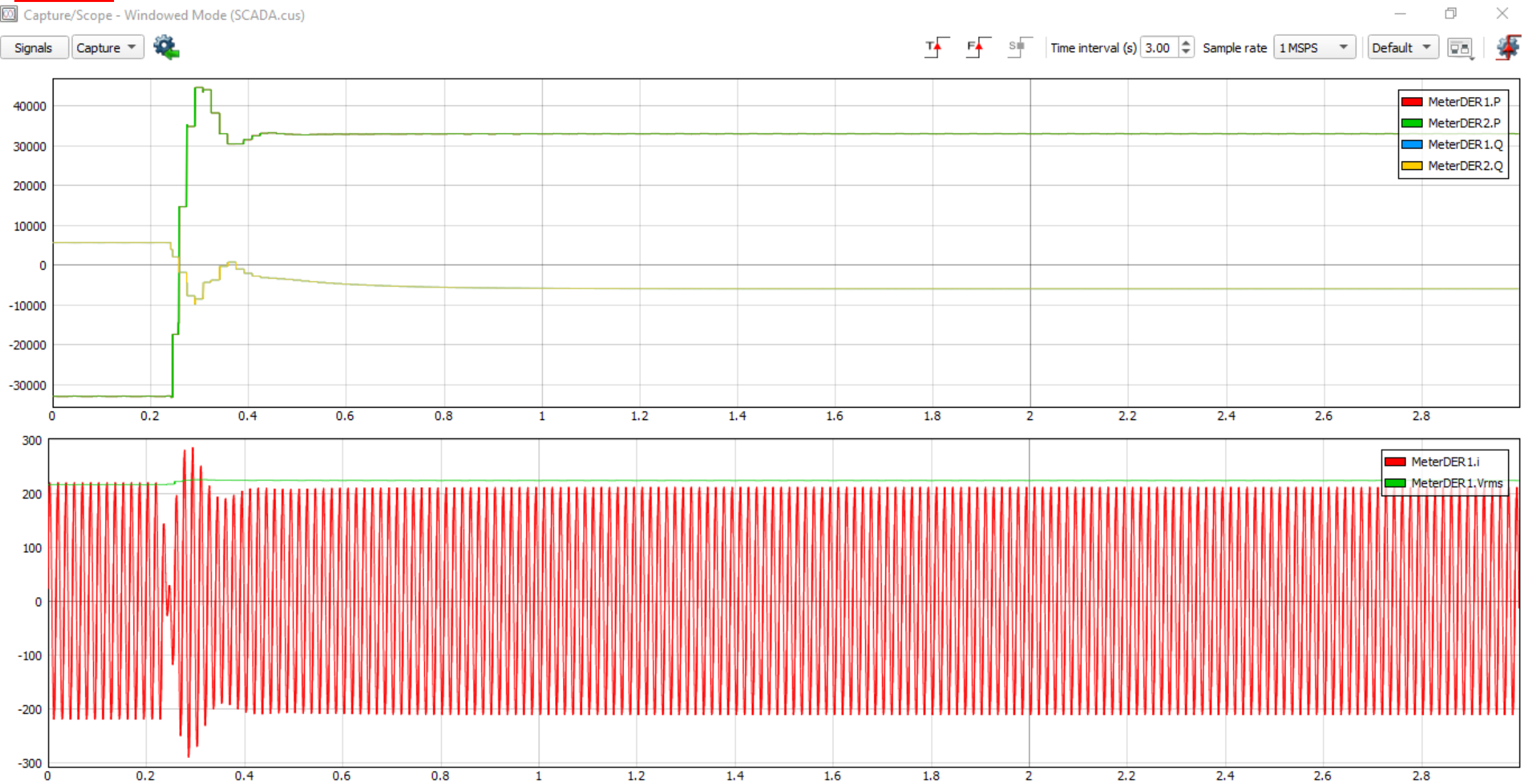
# Example

The association between the states on the modes can be seen from the participation factors:

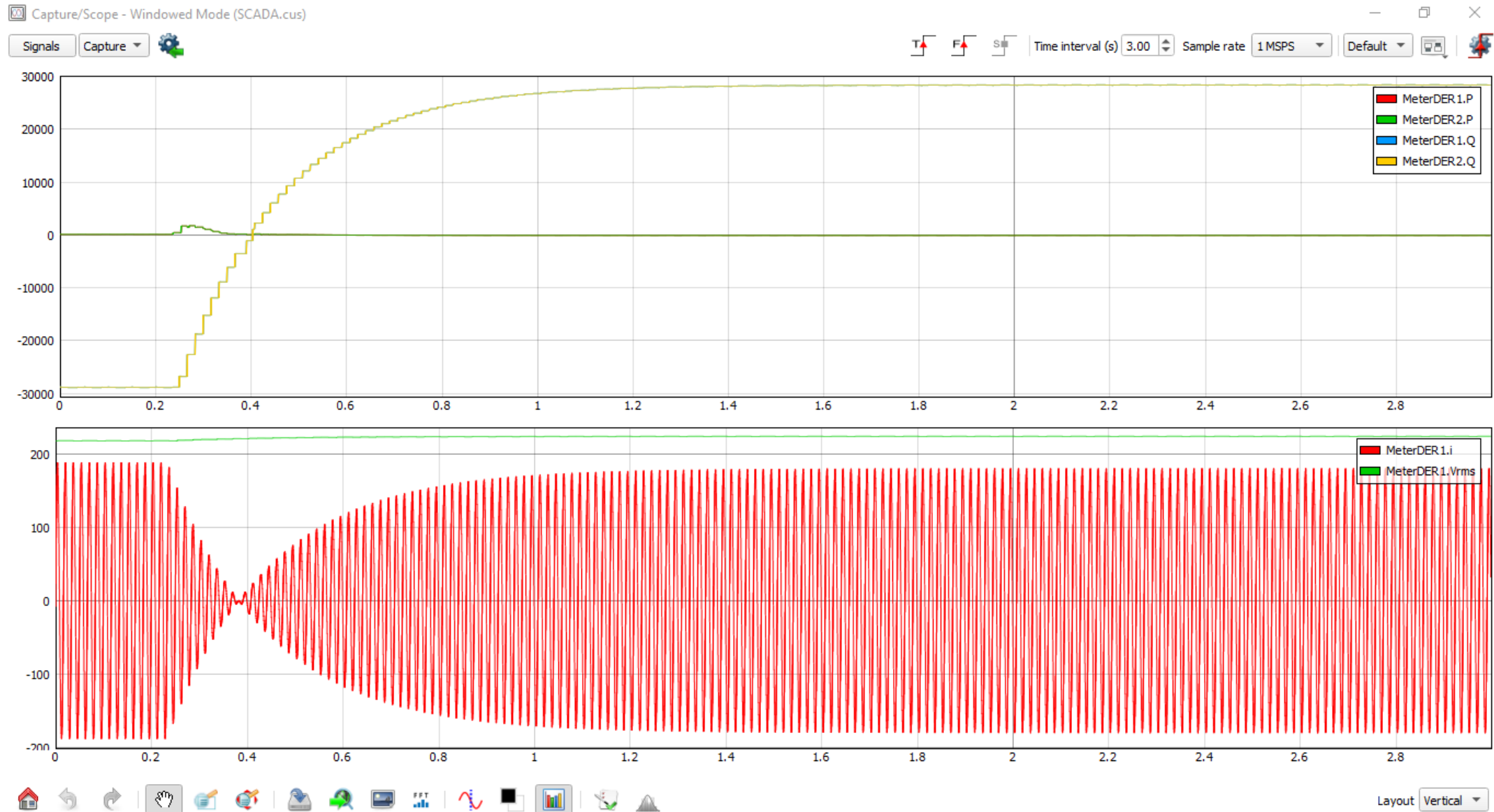
$$\begin{bmatrix} \lambda_1 \\ \lambda_2 \\ \lambda_3 \\ \lambda_4 \end{bmatrix} = \begin{bmatrix} -94.25 + j68.55 \\ -94.25 - j68.55 \\ -8.39 \\ -180.10 \end{bmatrix} \Rightarrow \begin{matrix} \lambda_1 & \lambda_2 & \lambda_3 & \lambda_4 \\ \begin{bmatrix} 0.86 & 0.86 & 0 & 0 \\ 0.86 & 0.86 & 0 & 0 \\ 0 & 0 & 0.05 & 1.058 \\ 0 & 0 & 1.058 & 0.05 \end{bmatrix} & \begin{matrix} \delta \\ \omega \\ e_d \\ e \end{matrix} \end{matrix}$$

$$\begin{aligned} k_v &= 20 \\ n &= 10\% \\ m &= 5\% \\ a &= 2\pi 30 \\ X_L &= 0.25 \text{ (pu)} \\ Q_o &= 0 \\ P_o &= 1 \text{ (pu)} \\ V &= 1 \text{ (pu)} \\ E_o &= 1 \text{ (pu)} \\ \omega_o &= 1 \text{ (pu)} \end{aligned}$$

# Transient Response

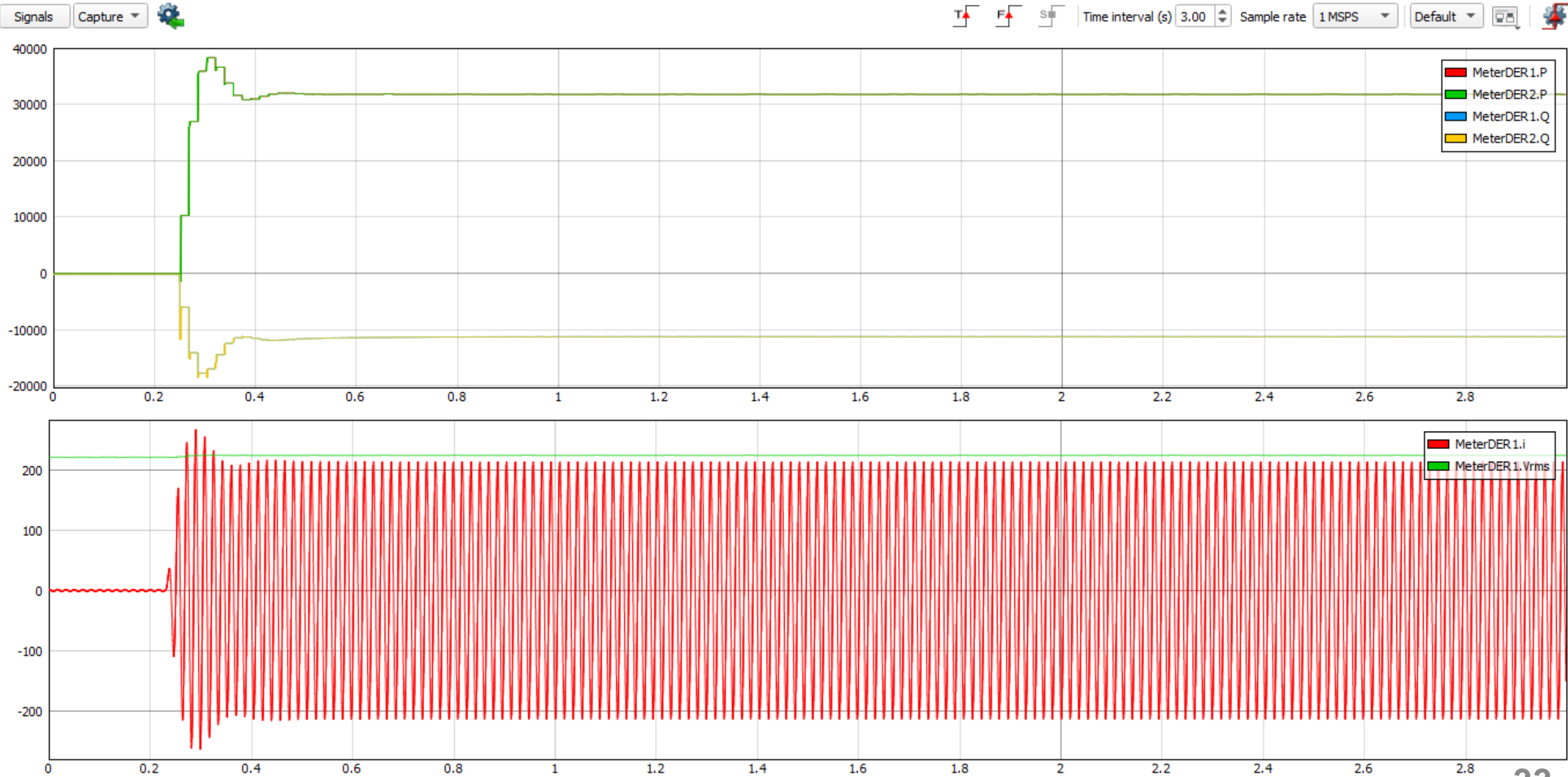


# Transient Response

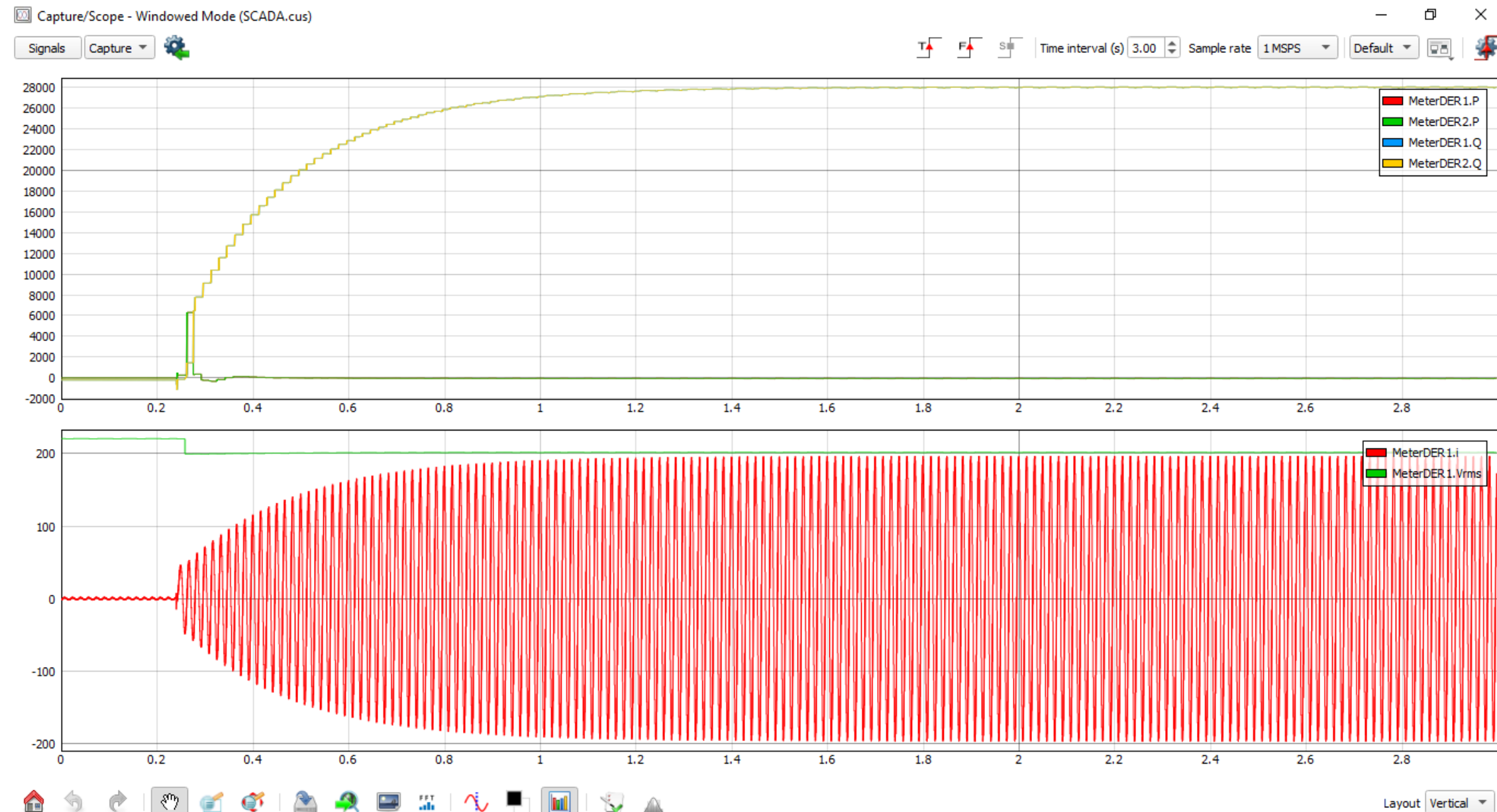


# Transient Response

Capture/Scope - Windowed Mode (SCADA.cus)



# Transient Response





# Summary

---

- ❑ With the use of a virtual inductor, the impact of the  $X/R$  ratio of the grid, seen from the PoC, is reduced.
- ❑ The selection of the droop coefficients impacts both the transient and steady-state behavior of the grid-forming inverter.
- ❑ For the derivation of small-signal analyzes of the grid-forming inverter with droop control, the inner voltage and current loops can be neglected.
- ❑ The use of an additional integrator in the reactive power voltage loop improves the droop characteristics in steady-state.
- ❑ The implementation of the droop control is straightforward.