

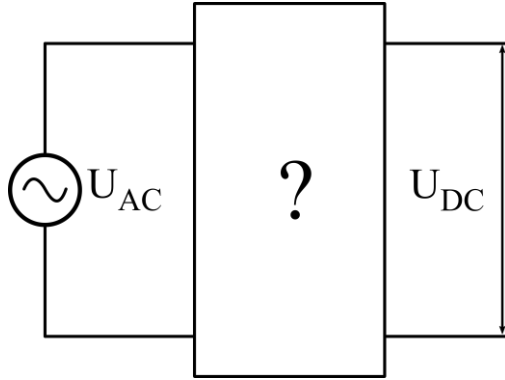
# RECTIFIERS

## SINGLE-PHASE RECTIFIERS

- What are rectifiers?
- Types of rectifiers.
- Single-phase diode rectifiers.
- Single-phase thyristor rectifiers.

# RECTIFIERS

What are rectifiers?



Rectifiers are devices that convert **AC** voltages/currents into **DC** voltages/currents.

Important note - they provide “either” small  $\Delta U_{DC}$  “or” small  $\Delta I_{DC}$ .

What is a DC and what is an AC variable?

Types of rectifiers:

Uncontrolled vs Controlled (vs Half/semi-controlled)

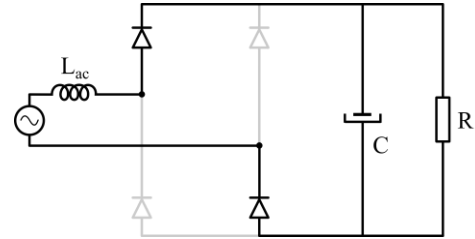
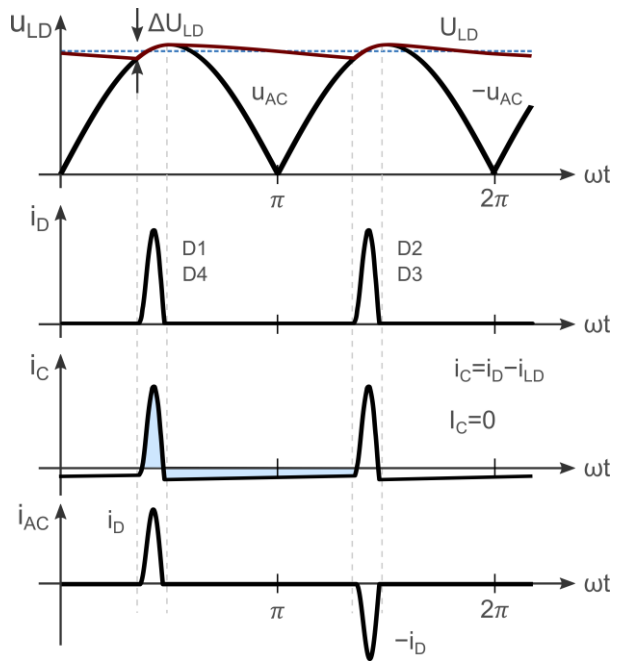
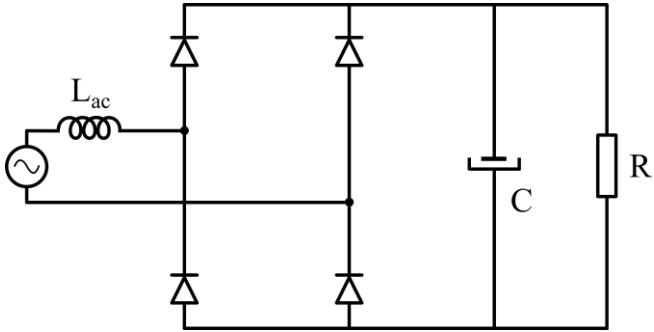
Single-phase vs Three-phase (vs Multi-phase)

Half-wave vs Full-wave

Voltage multipliers

# RECTIFIERS

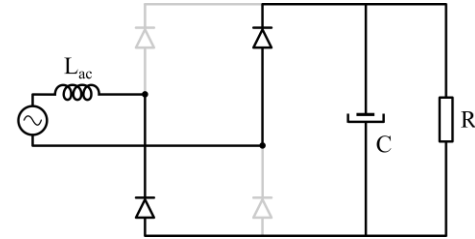
## Single-phase diode (uncontrolled) rectifier



$$U_{LDmax} = \sqrt{2} \cdot U_{AC} - 2 \cdot V_D$$

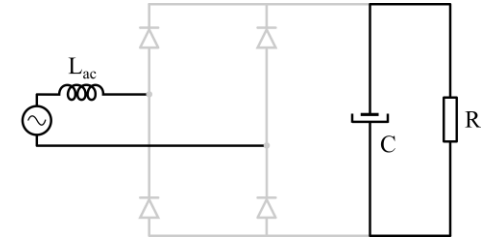
$$u_{LD} = u_{AC} - 2 \cdot V_D$$

$$i_C = i_D - i_{LD} \quad i_{AC} = i_D$$



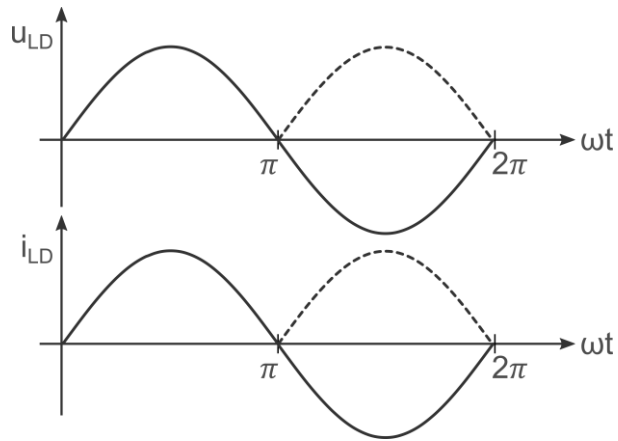
$$U_{LDmax} = \sqrt{2} \cdot U_{AC} - 2 \cdot V_D$$

$$i_C = i_D - i_{LD} \quad i_{AC} = -i_D$$



$$u_{DC} \approx U_{LDmax} \cdot e^{-\frac{\omega t - \frac{\pi}{2}}{\omega \cdot \tau}}, \tau = C \cdot R$$

$$i_C = -i_{LD} \quad i_{AC} = i_D = 0A$$



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## Single-phase diode (uncontrolled) rectifier

Direct start with a discharged capacitor:

Capacitor sizing:

Assumption -  $\Delta U_{LD} \ll U_{LD}$  ( $\Delta U_{LD} \approx 0$ )

$\Rightarrow i_{LD} \approx I_{LD}$  and the discharge time is (whole) 10ms.

$$\Rightarrow \Delta U_{LDmax} = \frac{Q}{C} = \frac{I_{LD} \cdot 10ms}{C} \text{ or } C = \frac{I_{LD} \cdot 10ms}{\Delta U_{LDmax}}$$

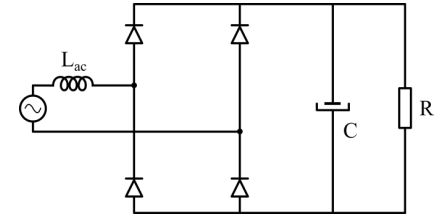
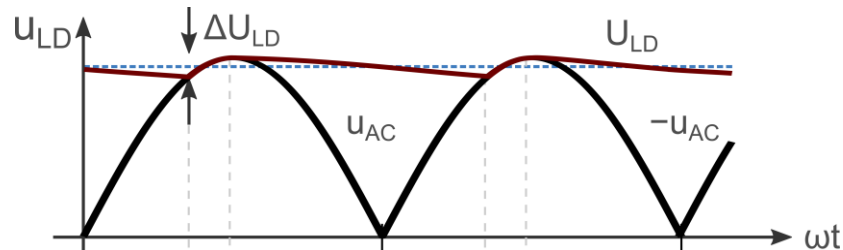
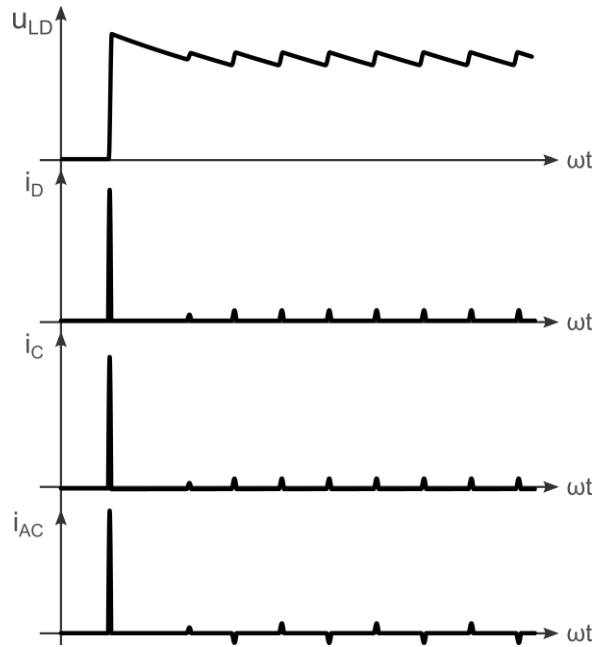
Example:

$$U_{AC} = 230V \text{ (50Hz)}, R = 150\Omega, C = 470\mu F$$

$$U_{LDmax} = \sqrt{2} \cdot 230V = 325V$$

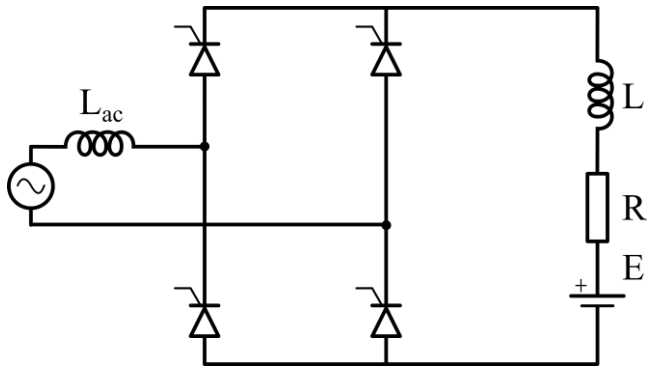
$$I_{LD} \approx \frac{U_{LDmax}}{R} = \frac{325V}{150\Omega} = 2,17A$$

$$\Delta U_{LD} = \frac{2,17 \cdot 10m}{470\mu} = 46V$$



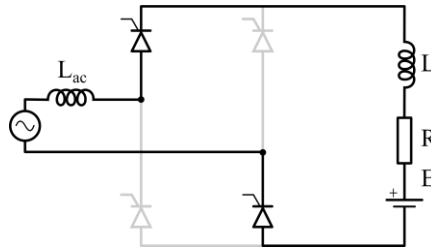
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## Single-phase thyristor (controlled) rectifier

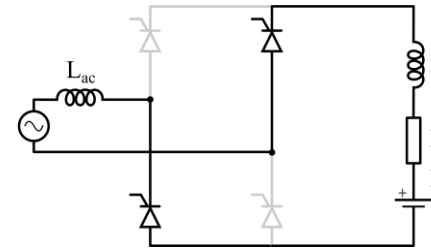


$$L \gg L_{ac} \Rightarrow u_{LAC} \ll$$

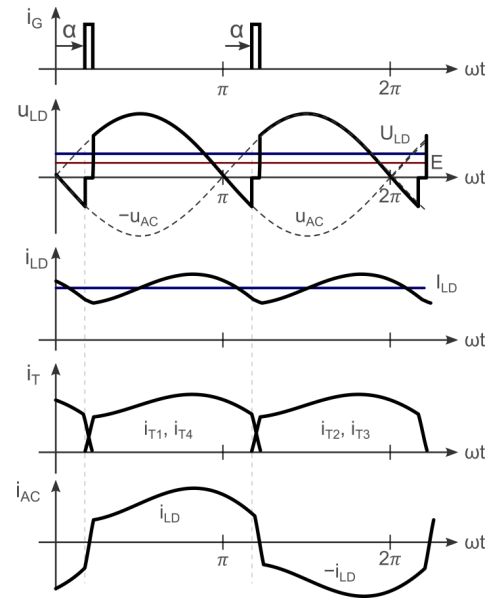
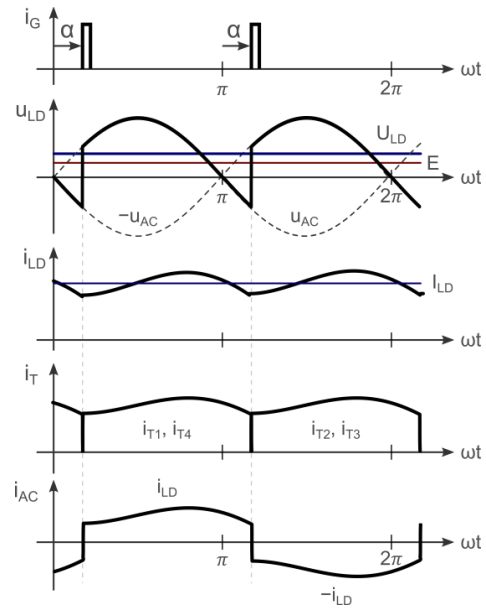
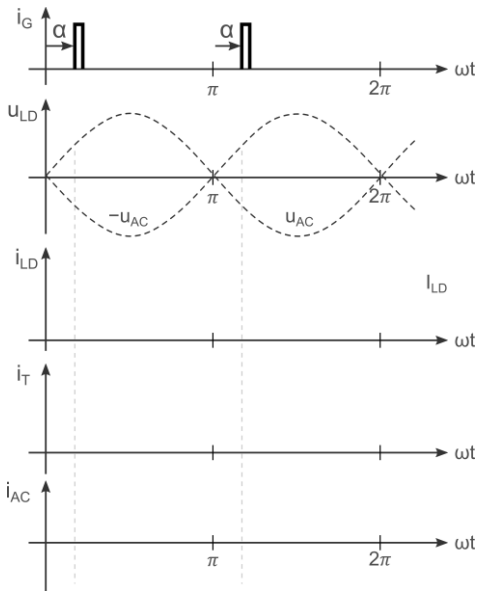
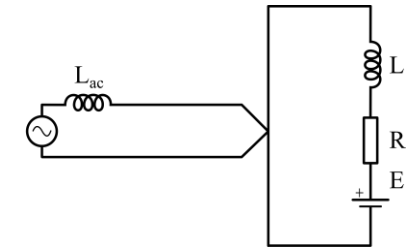
$$u_{LD} \approx u_{AC} \quad i_{AC} = i_{LD}$$



$$u_{LD} \approx -u_{AC} \quad i_{AC} = -i_{LD}$$



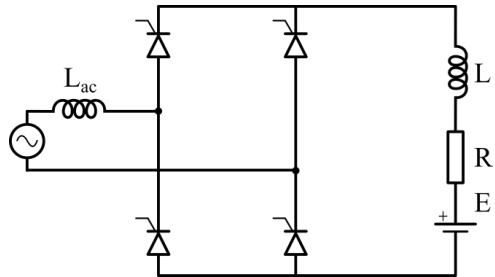
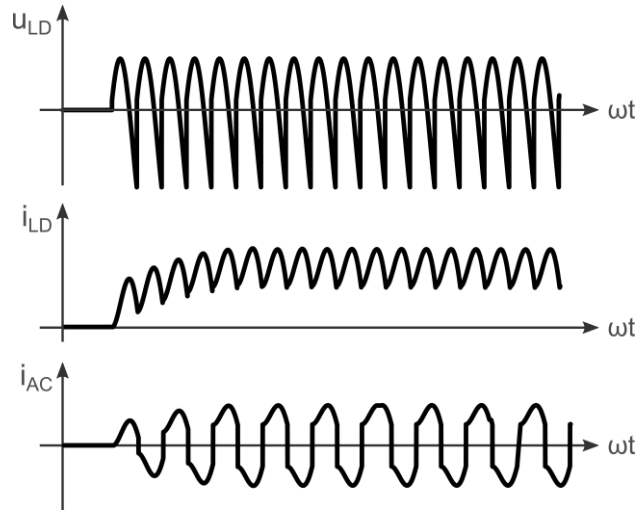
$$u_{LD} = 0V$$



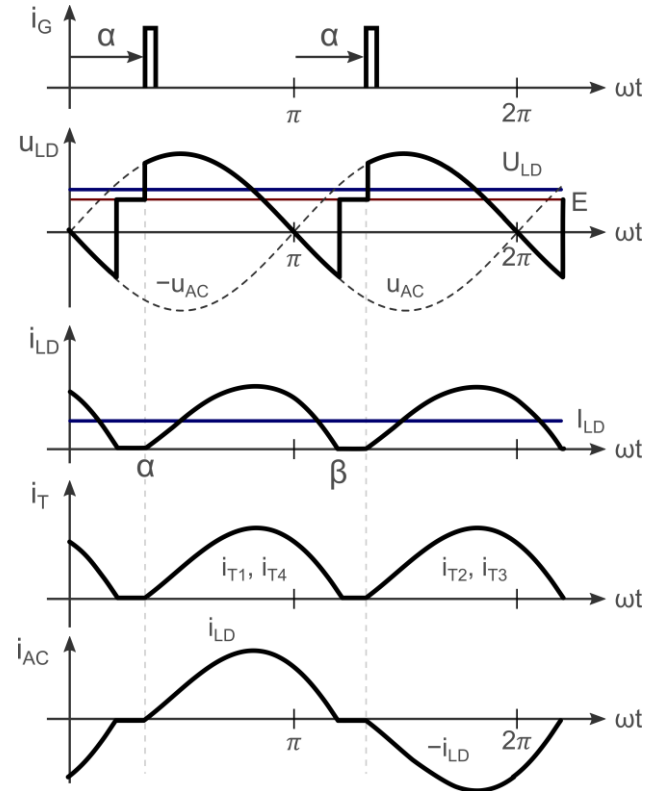
# RECTIFIERS

## Single-phase thyristor (controlled) rectifier

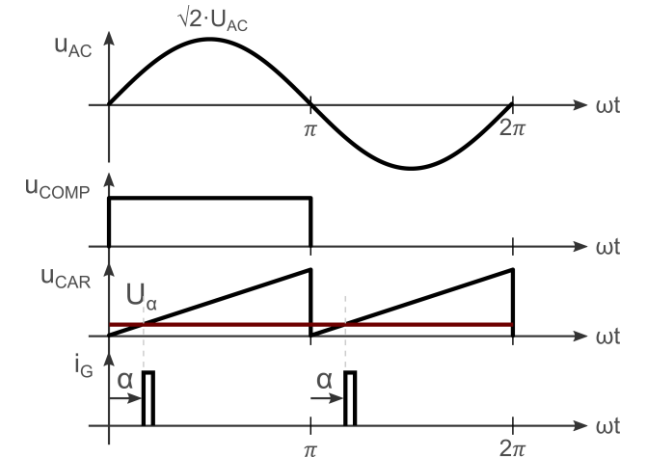
Direct start:



Discontinuous  $i_{LD}$ :



Synchronization:



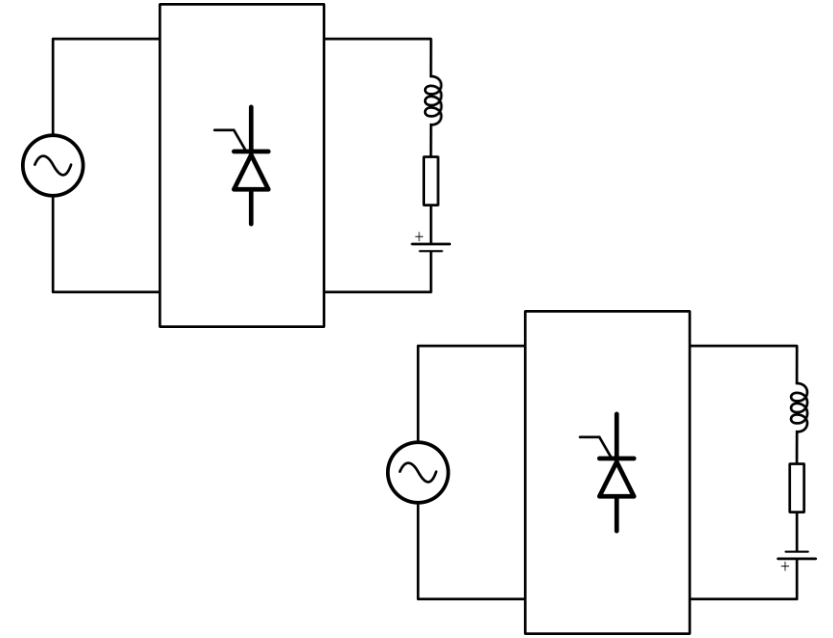
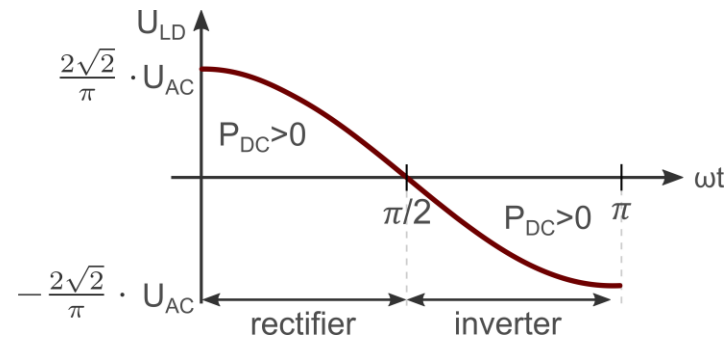
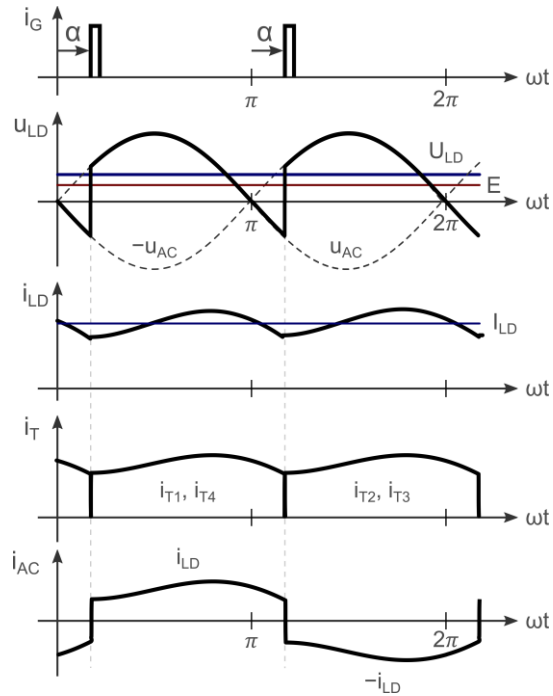
# RECTIFIERS

## Single-phase thyristor (controlled) rectifier

Continuous conduction mode  
(continuous  $i_{LD}$ ):

Average load voltage ( $U_{LD}$ ):

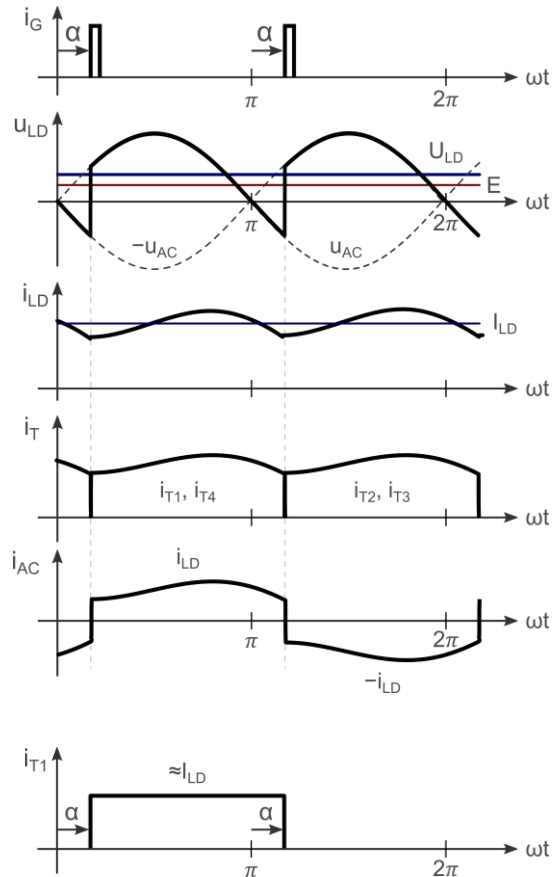
Average load current ( $I_{LD}$ ):



# RECTIFIERS

## Single-phase thyristor (controlled) rectifier

Continuous conduction mode  
(continuous  $i_{LD}$ ):



$$U_{AC} = 230V \text{ (50Hz)}, R = 5\Omega,$$

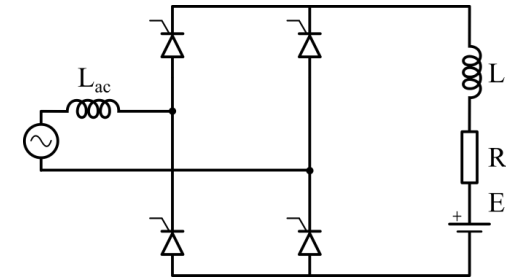
$$L = 100mH, E = 129,3V$$

Average load voltage - example:

$$U_{LD} = \frac{2\sqrt{2}}{\pi} \cdot U_{AC} \cdot \cos\alpha = \frac{2\sqrt{2}}{\pi} \cdot 230 \cdot \cos\left(\frac{\pi}{6}\right) = 179,3V$$

Average load current - example:

$$I_{LD} = \frac{U_{LD} - E}{R} = \frac{179,3 - 129,3}{5} = 10A$$



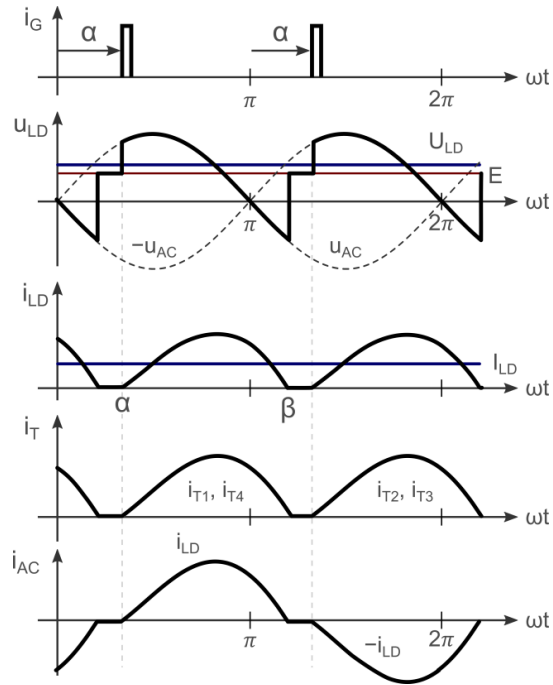
Choose thyristors:



# RECTIFIERS

## Single-phase thyristor (controlled) rectifier

Discontinuous conduction mode  
(discontinuous  $i_{LD}$ ):



Average load voltage ( $U_{LD}$ ):

$$U_{LD} = \frac{1}{\pi} \left[ \int_{\alpha}^{\beta} \sqrt{2} \cdot U_{AC} \cdot \sin(\omega t) \cdot d(\omega t) + \int_{\beta}^{\pi+\alpha} E \cdot d(\omega t) \right]$$

$$= \frac{\sqrt{2} \cdot U_{AC}}{\pi} \cdot [\cos \alpha - \cos \beta] + E \cdot \frac{\pi + \alpha - \beta}{\pi}$$

Load current ( $i_{LD}$ ):

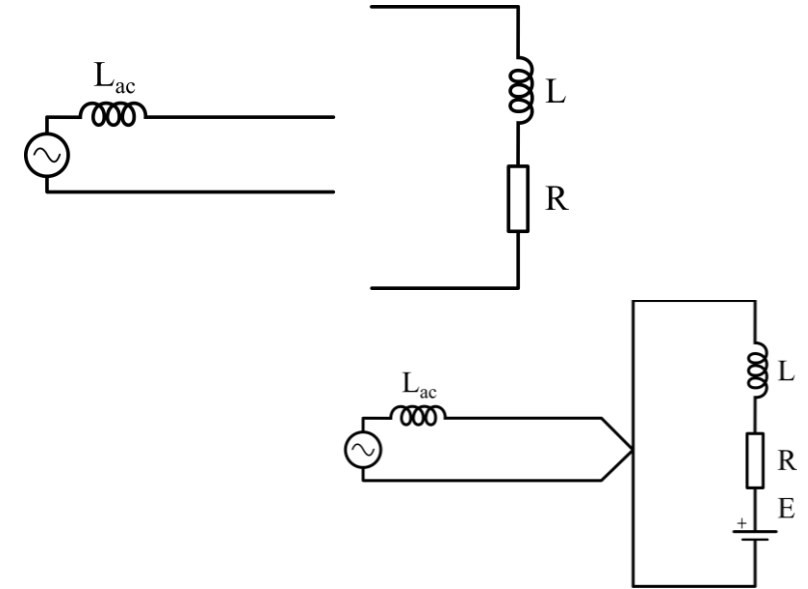
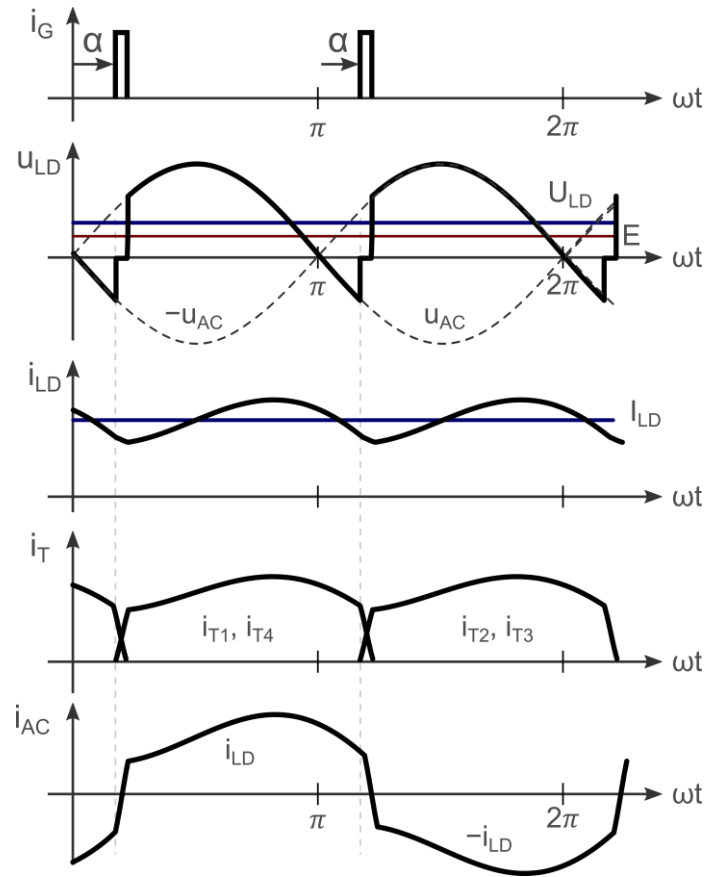
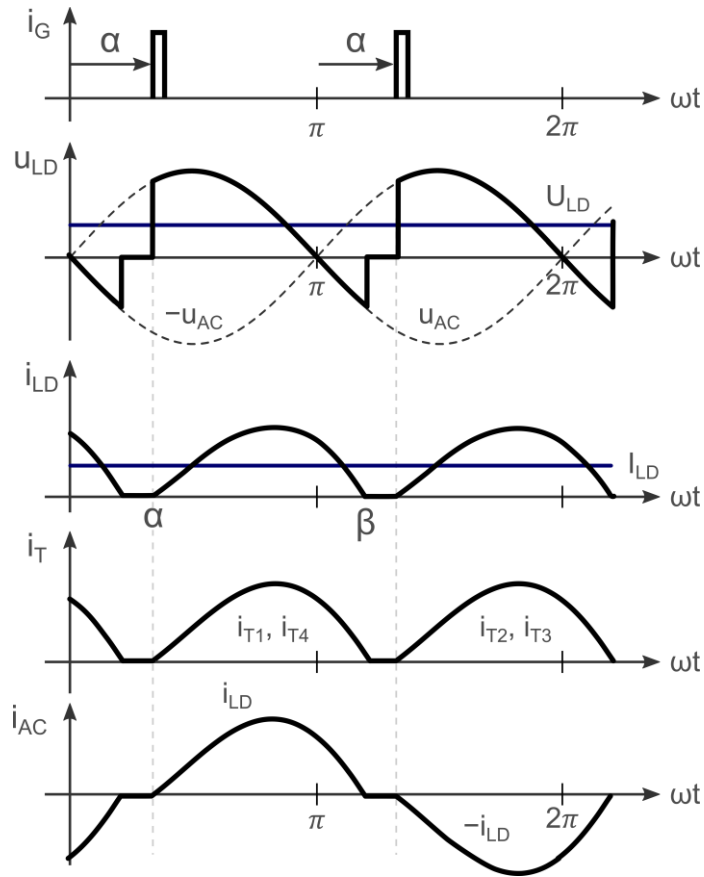
$$i_{LD} = A \cdot \sin(\omega t - \varphi) + B \cdot e^{-\frac{\omega t - \alpha}{\omega \tau}} + C$$

$$i_{LD}(\beta) = 0 \Rightarrow 0 = A \cdot \sin(\beta - \varphi) + B \cdot e^{-\frac{\beta - \alpha}{\omega \tau}} + C$$

# RECTIFIERS

## Single-phase thyristor (controlled) rectifier

Discontinuous conduction mode  
(discontinuous  $i_{LD}$ ):



# RECTIFIERS

## Single-phase rectifiers - important notes

- There are controlled and uncontrolled rectifiers,
- Filtering is extensively used,
- Filters influence the semiconductor devices conduction times,
- Diode bridge secures output voltage with small ripple,
- Thyristor bridge secures output current with small ripple,
- They drive different types of load,
- Load current can be discontinuous in thyristor bridges,
- Thyristor bridges necessitate synchronization unit,
- Comutation is process of importance for thyristor bridges,
- For continuous load current, the thyristor bridge can behave both as a rectifier and as an inverter (depending on firing angle).

